

**ECE 6744/ ME 6544/ AOE 6744: Linear Control Theory
Course Syllabus**

Instructor: Mazen Farhood
224-10 Randolph Hall
E-mail: farhood@vt.edu
Phone: 231-2983

Meeting Time: Tuesdays and Thursdays, 3:30 to 4:45 PM

Meeting Place: Whittimore 257

Office Hours: Tuesdays and Thursdays, 2:00 to 3:20 PM

Grader: Jean-Michel Fahmi (fahmi@vt.edu)

Description: This course covers optimal controller and observer design for multi-input, multi-output linear systems. Major course topics include a review of linear system theory, linear-quadratic optimal control theory, linear-quadratic Gaussian (optimal controller/observer) theory, and methods for ensuring robustness to model uncertainty and time delays.

References: Texts Focusing on Linear Optimal Control

P. Dorato, C. T. Abdallah, and V. Cerone. *Linear Quadratic Control: An Introduction*, Krieger Publishing.

B. D. O. Anderson and J. B. Moore. *Linear Optimal Control*, Prentice Hall, Englewood Cliffs, NJ, 1971.

R. W. Brockett. *Finite Dimensional Linear Systems*, John Wiley and Sons, New York, NY, 1970.

H. Kwakernaak and R. Sivan. *Linear Optimal Control Systems*, John Wiley and Sons, New York, NY 1972.

More General Texts on Optimal Control

A. E. Bryson, Jr. and Y.-C. Ho. *Applied Optimal Control: Optimization, Estimation, and Control*, (Revised Printing) Taylor and Francis, New York, NY 1975.

R. F. Stengel. *Optimal Control and Estimation*, Dover, New York, NY 1986.

Grade:	20%	Homework
	40%	Midterm Exam (24-hour take-home exam)
	40%	Final Exam (24-hour take-home exam)

Course Topics:

- I. Linear System Theory
 - A. Linear Algebra
 - i. Vector spaces and norms
 - ii. Linear maps; range and null space
 - iii. Existence and uniqueness of solutions to linear algebraic equations
 - iv. The eigenvalue problem
 - v. Symmetric matrices and quadratic forms
 - vi. Similarity transformations and the Jordan form
 - B. Linear ODEs
 - i. Linearization of nonlinear ODEs
 - ii. The state transition matrix
 - C. System Structural Properties
 - i. Controllability
 - ii. Observability
 - iii. Stability
- II. The Linear-Quadratic Controller
 - A. Derivation of the LQ controller by dynamic programming
 - i. Solution for time-varying systems
 - ii. Solution for time-invariant systems
 - iii. Steady-state (infinite horizon) solution for time-invariant systems (The Linear-Quadratic Regulator)
 - 1. Penalty matrix selection
 - 2. Guaranteed degree of stability
 - iv. LQ optimal trajectory tracking
 - B. Robustness of the LQR state feedback controller
 - i. Nyquist plots
 - ii. Stability (gain and phase) margins
- III. State Estimation and Output Feedback
 - A. Introduction to stochastic systems
 - B. The Kalman-Bucy filter
 - C. The LQG controller and the separation principle
 - D. Loss of robustness and loop transfer recovery